

```
In [1]:
         import Pkg
         Pkg.activate("../Tasks2D")
         Activating project at `~/Developer/tasks2D/Tasks2D`
In [2]:
         using Revise
                           # For development; makes it so modifications
                           # to imported modules are immediately reflected in this
         import LineWorlds # Local module with code for 2D maps where
                           # the primitive objects are line segments.
         const L = LineWorlds
         const Geo = L.Geometry;
In [3]:
         using Gen
In [4]:
         includet("KidnappedRobot/visualization.jl")
```

Define environment model

```
In [5]: ### Initial state distribution ###

mvuniform = L.ProductDistribution(uniform);
    @gen function uniform_agent_pos(params)
        mins, maxs = params.bounding_box
        pos ~ mvuniform(mins, maxs)

    return pos
end
```

DynamicDSLFunction{Any}(Dict{Symbol, Any}(), Dict{Symbol, Any}(), Type[An
y], false, Union{Nothing, Some{Any}}[nothing], var"##uniform_agent_pos#31
4", Bool[0], false)

```
### Transition model ###

# Load: `det_next_pos`, which computes the determinized effect of actions
# Load: `handle_wall_intersection` to handle wall intersections
includet("KidnappedRobot/motion_model_utils.jl")

# Motion model accepts the previous world state (the agent's previous pos.
# and an action in [:up, :down, :left, :right, :stay]
@gen function motion_model(prev_pos, action, params)

# Move the agent up/down/left/right by params.step.\(\Delta\) units.

np = det_next_pos(prev_pos, action, params.step.\(\Delta\))

# Have an affordance in the model for the agent to randomly
# re-locate to a new position.
is_kidnapped ~ bernoulli(params.p_kidnapped)

if !is_kidnapped
# In normal operation, the agent moves to `np`, plus
```

```
# a bit of stochastic noise.
pos ~ broadcasted_normal(np, params.step.o)

# If `np` plus the noise
# would have the agent collide with a wall, the agent
# halts preemptively.
next_pos = handle_wall_intersection(prev_pos, pos, params.map)

else
# If the robot was kidnapped, it could appear anywhere.
# {*} syntax inlines the random choices (here, `:pos`) from the
# `uniform_agent_pos` generative function into this one.
next_pos = {*} ~ uniform_agent_pos(params)
end

return next_pos
end
```

DynamicDSLFunction{Any}(Dict{Symbol, Any}(), Dict{Symbol, Any}(), Type[Any, Any, Any], false, Union{Nothing, Some{Any}}[nothing, nothing, nothing], var"##motion_model#315", Bool[0, 0, 0], false)

```
### Observation model ###

# Load: `get_sensor_args`; `sensordist_2dp3`.
includet("KidnappedRobot/sensor_model_utils.jl")

# This observation model generates noisy LIDAR measurements
# from the agent to the surrounding walls.
# See the visuals below.
@gen function sensor_model(pos, params)
    sensor_args = get_sensor_args(pos, params)
    obs ~ L.sensordist_2dp3(sensor_args...)
    return obs
end
```

DynamicDSLFunction{Any}(Dict{Symbol, Any}(), Dict{Symbol, Any}(), Type[Any,
Any], false, Union{Nothing, Some{Any}}[nothing, nothing], var"##sensor_mode
l#316", Bool[0, 0], false)

Define POMDP

```
In [8]:
        import GenPOMDPs
In [9]:
        # POMDP of this environment
        pomdp = GenPOMDPs.GenPOMDP(
            uniform_agent_pos,
                                    # INIT
                                             : params
                                                                           → sta
            motion_model,
                                   # STEP
                                             : prev_state, action, params → stat
            sensor model,
                                   # 0BS
                                             : state, params
                                                                          → obse
            (state, action) → −1. # UTILITY: state, action, params
                                                                           → uti
                                    # "→" denotes a Generative Function: "→" den
        )
```

GenPOMDPs.GenPOMDP(DynamicDSLFunction{Any}(Dict{Symbol, Any}(), Dict{Symbol, Any}(), Type[Any], false, Union{Nothing, Some{Any}}[nothing], var"##unif
orm agent nos#314". Bool[0]. false). DynamicDSLFunction{Any}(Dict{Symbol. A

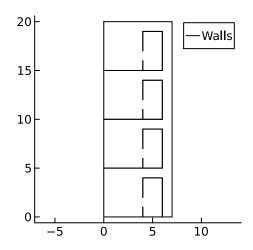
ny}(), Dict{Symbol, Any}(), Type[Any, Any, Any], false, Union{Nothing, Some
{Any}}[nothing, nothing, nothing], var"##motion_model#315", Bool[0, 0, 0],
false), DynamicDSLFunction{Any}(Dict{Symbol, Any}(), Dict{Symbol, Any}(), T
ype[Any, Any], false, Union{Nothing, Some{Any}}[nothing, nothing], var"##se
nsor_model#316", Bool[0, 0], false), var"#35#36"())

Load an environment

```
# Load function to construct a "hotel" map with a given number
# of identical rooms.
includet("KidnappedRobot/hotel_env.jl")

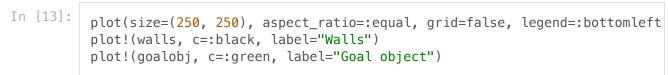
# Construct a hotel environment with 4 rooms.
(walls, bounding_box) = construct_hotel_env(4);
```

```
plot(size=(250, 250), aspect_ratio=:equal, grid=false)
plot!(walls, c=:black, label="Walls")
```

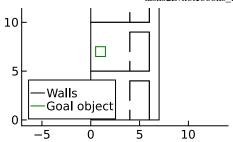


Add goal object to environment

```
includet("KidnappedRobot/box.jl") # get `box_segments`, which draws a box
# Coordinates for where to place goal object in the map we loaded above
GOAL = [1., 7.]
goalobj = box_segments(GOAL);
```







Ground truth world parameters

```
In [14]:
          ### Ground truth world model parameters ###
          PARAMS = (:
              map = vcat(walls, goalobj),
                                                # The map consists of the walls, and
              p_kidnapped = 0.,
                                                 # Probability the agent is kidnapped
                                                # Bounding box for the environment
              bounding box = bounding box,
              step = (; \Delta = 0.25, \sigma = 0.005), # step model arguments
              obs = (; fov = 2\pi, n_rays = 80, # obs model arguments
                  orientation=\pi/2,
                  sensor_args = (;
                       w = 5, s_noise = 0.02,
                       outlier = 0.0001, outlier vol = 100.0,
                       zmax = 100.0
          )));
```

Construct a particle filter

Next, we'll construct a 1-particle particle filter we can use for state estimation in this model. It will be based on a proposal distribution which uses a coarse-to-fine sequence of grid scans over the 2D environment to precisely localize the agent.

```
In [15]:
          ### Particle Filter args ###
          # pf.jl defines `@get_pf`. This macro simply yields a call `GenPOMDPs.pf
          # grid proposal distribution.
          # `GenPOMDPs.pf` is a function which accepts a POMDP as input, and parame
          # behavior of a particle filter, and constructs a particle filter special
          # of all POMDPs.
          # `pf.jl` also defines some particle filtering proposal distributions base
          # coarse-to-fine grid scans.
          includet("KidnappedRobot/pf.jl")
          # Also load a file where I defined some default arguments for the particle
          # proposal distributions.
          includet("KidnappedRobot/default_pf_args.jl")
          # Construct the POMDP the agent will use as it's mental world model while
          # In this case, the mental-model GenPOMDP object will be the same as the
          # However, the exact distributions represented by the mental-model POMDP
          # be different, since we will give the agent a different set of parameter:
```

```
# (I could potentially refactor GenPOMDPs so that the GenPOMDP object con
# rather than the user passing this in each time. That would also more p
# formal definition of a POMDP. However, I had in mind it may be convenient
# to have an explicit `params` argument which can control details of the (
agent_mental_model = GenPOMDPs.GenPOMDP(uniform_agent_pos, motion_model,
# [We could just set agent mental model = pomdp; I write this out for ill
# We will have the agent's mental model suppose the
# motion noise and observation noise are higher than
# they truly are, and the agent will do particle filtering
# assuming kidnapping is impossible. (The controller will handle
# kidnapping by resetting the particle filter.)
MENTAL MODEL PARAMS = overwrite params(
    PARAMS;
    p kidnapped=0.,
    step=(; \sigma = 0.1),
    sensor_args=(; s_noise=0.1)
)
# Arguments for 1 particle SMC. [The resampling args don't do anything, s.
update_grid_args, initialization_grid_args, resampling_args = default_pf_
# Particle filter for inference in the mental world model
pf = @get_pf(agent_mental_model, MENTAL_MODEL_PARAMS, update_grid_args, i
# The particle filter object returned by GenPOMDPs.pf is a pair of a func
# which initializes a particle filter, `initial_pf_state = pf_init(observation)
# which updates the filter, `new_pf_state = pf_update(pf_state, action, new_pf_state)
(pf_init, pf_update) = pf;
```

```
In [16]: # In inference, we'll use this generative function by constructing a Conti
# GenPOMDPs.RolloutModel(pomdp, controller)
ctm = GenPOMDPs.ControlledTrajectoryModel(agent_mental_model)
ctm isa Gen.GenerativeFunction
```

true

Baseline controller

As a baseline, we'll implement a controller which does state estimation without a particle filter; it will simply do a coarse-to-fine grid scan over the entire map to localize globally at every timestep.

To implement this, we'll simply use the pf init function we obtained above when

constructing our particle filter. That is, we will construct a 1-particle filter at every timestep, as though each new observation is the first observation.

For planning, we'll do A* search in a discretized version of the environment. To do this, our first step will be to construct a "GridWorld" environment, by overlaying a cartesian grid onto the continuous environment, and noting which squares in the grid are occupied by walls.

```
includet("KidnappedRobot/astar_planning.jl") # Loads: `find_action_using_
# Generate a gridworld version of this environment, in which A* planning
planning_params = get_planning_params(walls, bounding_box);
```

Then, we'll define the controller.

```
In [19]:
          includet("KidnappedRobot/handle_sticking.jl") # Loads: `handle_sticking`
          @gen function _baseline_controller(controller_state, obs)
              (prev pf state, prev action) = controller state
              # Do a global localization scan, based on the current timestep's obse
              # Ignore any past inferences.
              pf_state = pf_init(choicemap((:obs, obs)))
              # Plan a trajectory to the goal in that grid contained in `planning pe
              # Return the first action of that plan.
              action = find_action_using_grid_search(planning_params, currentpos(pf)
              # Sometimes, the details of the motion model and the A* planning
              # can cause the agent to "stick" on the walls.
              # This `handle_sticking` function checks if the agent has been trying
              # to perform the same action for multiple timesteps, but its belief s
              # has not changed; if so, it takes a random action orthogonal to the
              # action that is causing sticking.
              action = handle_sticking(prev_pf_state, prev_action, pf_state, action
              return (action, (pf_state, prev_action)) # (action, next_controller_s
          end
          baseline_controller = GenPOMDPs.Controller(
              baseline controller, # Controller state, observation → action, next
              (nothing, nothing) # Initial controller state
          )
```

GenPOMDPs.Controller(DynamicDSLFunction{Any}(Dict{Symbol, Any}(), Dict{Symbol, Any}(), Type[Any, Any], false, Union{Nothing, Some{Any}}[nothing, nothing], var"##_baseline_controller#709", Bool[0, 0], false), (nothing, nothing))

Now that we have defined the controller, we can get a Generative Function over trajectories from rolling out the true world model, using this controller to choose actions.

The arguments to this generative function are T, the number of timesteps to roll out,

and the POMDP parameters.

```
In [20]:
          baseline_rollout_model = GenPOMDPs.RolloutModel(pomdp, baseline_controlle
        GenPOMDPs.var"##StaticGenFunction RolloutModel#778"(Dict{Symbol, Any}(), D
        ict{Symbol, Any}())
         Now let's simulate from this model.
         First, we'll generate just the initial timestep.
In [21]:
          # Start the agent off in a hallway.
          INITIAL POS = [6.5, 4*5 - 2];
In [22]:
          baseline rollout tr = Gen.generate(baseline rollout model, # Generate a
              (0, PARAMS),
                                                                       # ...up to til
              choicemap((GenPOMDPs.state_addr(0, :pos), INITIAL_POS)) # ...and cons
          )[1];
          trace_to_gif(baseline_rollout_tr; goalobj=goalobj) # Visualize the rollou
          Info: Saved animation to /tmp/jl_kdcr6dutcD.gif
        L @ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156
            True World State
                                              Agent Beliefs
```

Now, we'll have the model simulate behavior for 100 timesteps.

Observed distances from LIDAR

True agent position

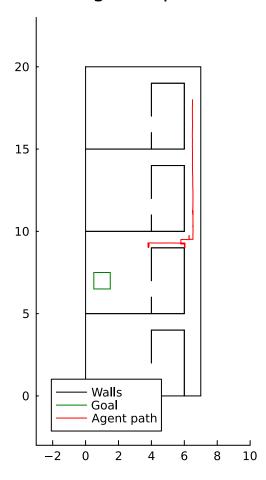
LIDAR dists rel. to belief

Goal

Belief: possible agent location

Goal

Agent's path



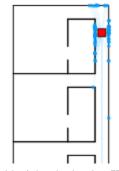
Here's a video of the agent's position and belief, over time.

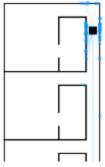
In [24]: trace_to_gif(baseline_rollout_tr; goalobj=goalobj, fps=10)

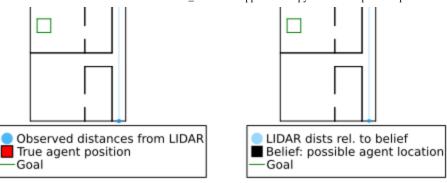
Info: Saved animation to /tmp/jl_qb4lMBsPWp.gif
@ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156

True World State

Agent Beliefs







The issue with this controller is that it does not remember its belief from the last timestep; it tries to fully relocalize at every step just using its current observations.

The result is that when the agent moves into a hallway into one of the rooms (which looks just like the hallways that lead into each other room), the agent gets confused about where it is. The issue is that the observed data from that timestep alone does not dis-ambiguate where the object is. At each timestep it thinks it is in the hallway toward the goal, it takes a step into the room; at each timestep it thinks it is in another hallway, it takes a step out from the room. As a result, it keeps going back and forth, and is stuck!

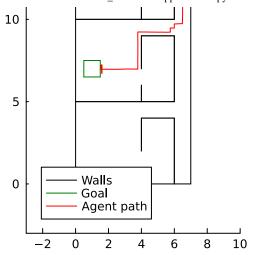
Baseline particle-filtering controller

To fix this, let's use a controller which uses a 1-particle particle filter, rather than relocalizing at each timestep.

```
In [25]:
          @gen function _baseline_pf_controller(controller_state, obs)
              (prev_pf_state, prev_action) = controller_state
              if isnothing(prev pf state)
                  pf_state = pf_init(choicemap((:obs, obs)))
              else
                  pf_state = pf_update(prev_pf_state, prev_action, choicemap((:obs,
              end
              action = find_action_using_grid_search(planning_params, currentpos(pf)
              action = handle_sticking(prev_pf_state, prev_action, pf_state, action
              return (action, (pf_state, action)) # (action, next_controller_state)
          end
          baseline pf controller = GenPOMDPs.Controller(
              _baseline_pf_controller, # Controller state, observation → action, nex
              (nothing, nothing)
                                       # Initial controller state
          )
```

GenPOMDPs.Controller(DynamicDSLFunction{Any}(Dict{Symbol, Any}(), Dict{Symbol, Any}(), Type[Any, Any], false, Union{Nothing, Some{Any}}[nothing, nothing], var"##_baseline_pf_controller#1208", Bool[0, 0], false), (nothing, nothing))

```
In [26]:
          baseline_pf_rollout_model = GenPOMDPs.RolloutModel(pomdp, baseline_pf_con-
        GenPOMDPs.var"##StaticGenFunction__RolloutModel#1277"(Dict{Symbol, Any}(),
        Dict{Symbol, Any}())
In [27]:
          baseline_pf_rollout_tr = Gen.generate(baseline_pf_rollout_model, (0, PARA)
              choicemap((GenPOMDPs.state_addr(0, :pos), INITIAL_POS))
          )[1]
          trace_to_gif(baseline_pf_rollout_tr; goalobj=goalobj, title="First timeste
          Info: Saved animation to /tmp/jl_STW54HgPQ5.gif
        Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156
              First timestep
                                               First timestep
               Observed distances from LIDAR
                                                LIDAR dists rel. to belief
               True agent position
                                               Belief: possible agent location
                Goal
                                                Goal
In [28]:
          baseline_pf_rollout_tr, _ = Gen.update(baseline_pf_rollout_tr, (100, PARA)
          trace_to_path_image(baseline_pf_rollout_tr; goalobj=goalobj)
                                 Agent's path
                        20
                         15
```



In [29]: trace_to_gif(baseline_pf_rollout_tr; goalobj=goalobj, fps=10)

Info: Saved animation to /tmp/jl_etGps5Klq7.gif
@ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156
True World State Agent Beliefs

Observed distances from LIDAR True agent position Goal LIDAR dists rel. to belief Belief: possible agent location Goal

"Kidnap the robot"

Now, we'll give the robot the same task: navigate to the green square.

But, after 40 timesteps, we'll imagine the robot comes across a well-meaning hotel employee who sees the robot, and doesn't realize we roboticists have it doing an important task for us. The employee turns off the employee and brings it to a storage closet in one of the unoccupied hotel rooms. Eventually, we notice this issue, and we turn the robot back on. The robot controller then tries to pick up where it left off, and

find a path to the goal. But with the basic PF controller we defined above, the robot cannot re-localize after it is moved to a new place!

Info: Saved animation to /tmp/jl_AVcZWFY9kF.gif
@ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156

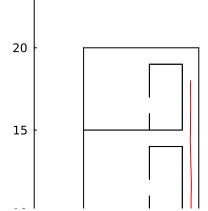
First timestep

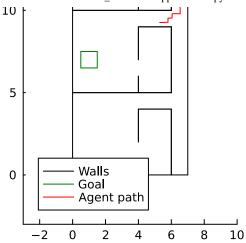
First timestep



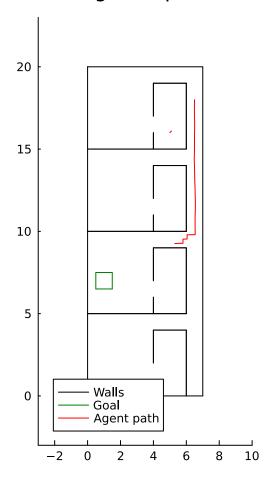
Extend rollout to 40 steps...
baseline_rollout_tr_KR, _ = Gen.update(baseline_rollout_tr_KR, (40, PARAMS
trace_to_path_image(baseline_rollout_tr_KR; goalobj=goalobj)

Agent's path





Agent's path

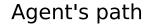


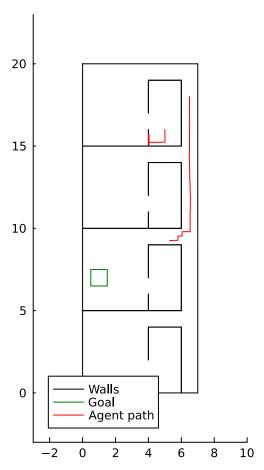
Roll out the trace another 100 steps, after the robot is re-activated.

baseline_rollout_tr_KR, _ = Gen.update(baseline_rollout_tr_KR, (140, PARAI)

trace_to_path_image(baseline_rollout_tr_KP, gealphi-gealphi_kidpapped_at-







In [34]: trace_to_gif(baseline_rollout_tr_KR; goalobj=goalobj, fps=10, kidnapped_a

Info: Saved animation to /tmp/jl_obmH4JotW9.gif
@ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156

True World State

Agent Beliefs



—Goal —Goal

The particle filter can't handle the robot kidnapping.

One solution would be to have the agent do expensive MCMC rejuvenation at every step, to check if it might have been moved elsewhere.

But we don't need to take on this computational cost. Instead, we can have the controller make intelligent decisions about on which steps we should spend more computation to re-localize globally.

Below, we'll implement a simple version of this, which resets the particle filter whenever the marginal likelihood estimate from the particle filter (the average particle weight -- and in this case the only particle weight) falls too low.

Robust controller: particle filtering + reset particle filter when the likelihood falls too low

```
In [35]:
          # @dist labeled_categorical(labels, probs) = labels[categorical(probs)]
In [36]:
          @gen function controller(controller state, obs)
              prev_pf_state, prev_action = controller_state
              # Create 1-particle belief state
              if isnothing(prev action) # First timestep
                  pf_state = pf_init(choicemap((:obs, obs)))
              else
                  # Log marginal likelihood estimate from the particle filter
                  prev_lml_est = GenParticleFilters.get_lml_est(prev_pf_state)
                  # Try updating the PF belief state
                  pf_state = pf_update(prev_pf_state, prev_action, choicemap((:obs,
                  new_lml_est = GenParticleFilters.get_lml_est(pf_state)
                  # We will define and tune this check below
                  if incremental_log_likelihood_est_is_too_low(new_lml_est - prev_lr
                      # Reset the particle filter!
                      # The new pf_state will be over trajectories of length 1.
                      pf_state = pf_init(choicemap((:obs, obs)))
                  end
              end
              # Choose action
              action = find_action_using_grid_search(planning_params, currentpos(pf)
              action = handle_sticking(prev_pf_state, prev_action, pf_state, action
              # Choose the action to take.
              # is_viable_onehot = [a in viable_actions ? 1. : 0 for a in [:left, :|
              # action probs = is viable onehot / sum(is viable onehot)
              # action ~ labeled_categorical([:left, :right, :up, :down, :stay], ac
```

```
return (action, (pf_state, action)) # (action, next_controller_state)
end

controller = GenPOMDPs.Controller(
    __controller, # Controller state, observation → accontroller, # Initial controller state
)
```

GenPOMDPs.Controller(DynamicDSLFunction{Any}(Dict{Symbol, Any}(), Dict{Symbol, Any}(), Type[Any, Any], false, Union{Nothing, Some{Any}}[nothing, nothing], var"##_controller#1901", Bool[0, 0], false), (nothing, nothing))

Tuning the particle filter log marginal likelihood threshold.

Now, we need to define incremental_log_likelihood_est_is_too_low , which we used in the controller above. This will be a simple threshold on the estimated value of $P(obs \mid latent_{t-1})$ from the particle filter.

Note that the expected value of P(obs) is $P(obs \mid latent)$. Based on this observation, we will set our threshold by generating 1000 random (latent, obs) pairs from the model, and setting the threshold to be the minimum value of $P(obs \mid latent)$ which arises.

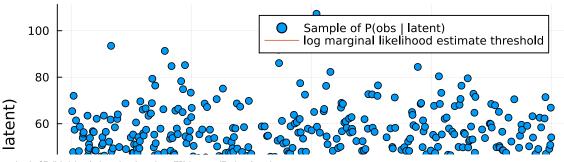
This is currently just a heuristic I quickly thought of to set this threshold, which I have observed works well in this environment. One of my research TODOs is to think more carefully about about whether this method of tuning the threshold can be expected to work well across environments.

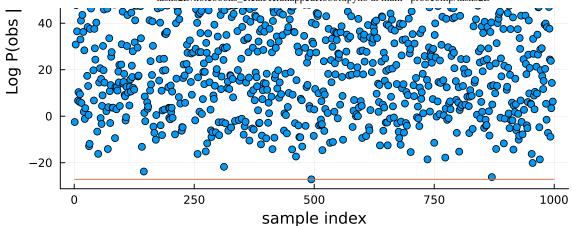
```
In [37]: logpy_values = []
for _=1:1000
    state = uniform_agent_pos(MENTAL_MODEL_PARAMS)
    obs_tr = simulate(sensor_model, (state, MENTAL_MODEL_PARAMS))
    push!(logpy_values, get_score(obs_tr))
end

logpy_threshold = minimum(logpy_values)

function incremental_log_likelihood_est_is_too_low(incremental_logpy_estimental_logpy_estimental_logpy_estimental_logpy_threshold
end

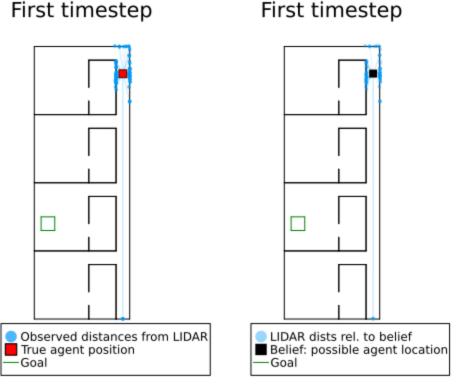
scatter(1:1000, logpy_values, ylabel="Log P(obs | latent)", xlabel="sample plot!(1:1000, [logpy_threshold for _=1:1000], label="log marginal likelihom")
```





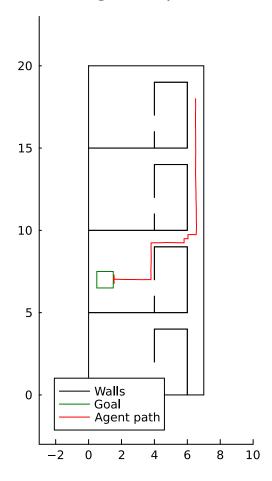
Simulating the robust controller, in an environment with no robot kidnapping.

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@ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156



```
# Extend rollout...
rollout_tr, _ = Gen.update(rollout_tr, (80, PARAMS), (UnknownChange(), Not
trace_to_path_image(rollout_tr; goalobj=goalobj)
```

Agent's path

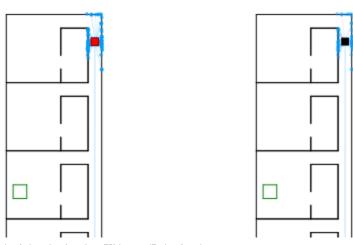


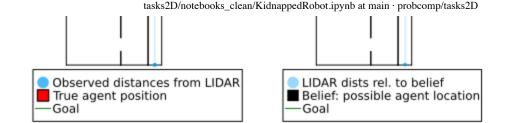
In [45]: trace_to_gif(rollout_tr; goalobj=goalobj, fps=10)

Info: Saved animation to /tmp/jl_8BIlKn8lcP.gif
@ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156

True World State

Agent Beliefs

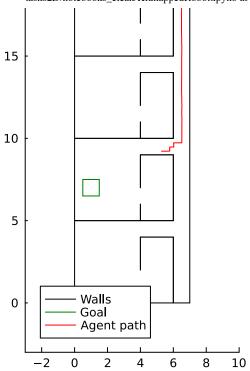




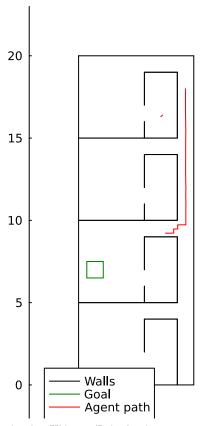
Kidnapped robot with the robust controller

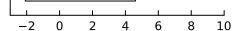
```
In [46]:
           robust_rollout_tr_KR = Gen.generate(rollout_model, (0, PARAMS),
                choicemap((GenPOMDPs.state_addr(0, :pos), INITIAL_POS))
           )[1]
           trace_to_gif(robust_rollout_tr_KR; goalobj=goalobj, title="First timestep"
         Info: Saved animation to /tmp/jl_wfaZwnYxep.gif
@ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156
               First timestep
                                                   First timestep
                Observed distances from LIDAR
                                                    LIDAR dists rel. to belief
                True agent position
                                                  Belief: possible agent location
In [47]:
           # Extend rollout to 40 steps...
           robust_rollout_tr_KR, _ = Gen.update(robust_rollout_tr_KR, (40, PARAMS),
           trace_to_path_image(robust_rollout_tr_KR; goalobj=goalobj)
                                    Agent's path
```

20



Agent's path

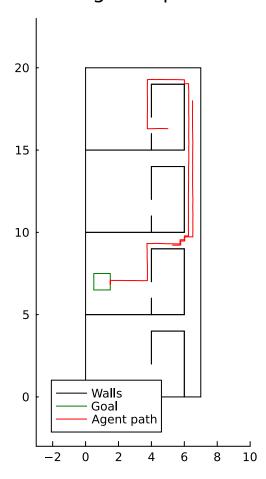




In [49]:

Roll out the trace another 100 steps
robust_rollout_tr_KR, _ = Gen.update(robust_rollout_tr_KR, (140, PARAMS),
trace_to_path_image(robust_rollout_tr_KR; goalobj=goalobj, kidnapped_at=[4]

Agent's path



In [50]:

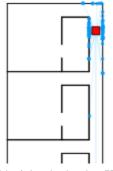
trace_to_gif(robust_rollout_tr_KR; goalobj=goalobj, fps=10, kidnapped_at=

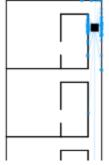
 $_{\Gamma}$ Info: Saved animation to /home/ubuntu/Developer/tasks2D/notebooks_clean/k_idnapping_recovery.gif.gif

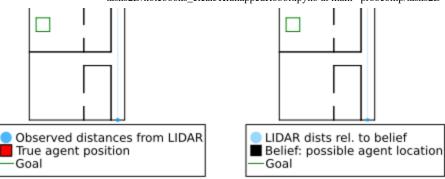
L @ Plots /home/ubuntu/.julia/packages/Plots/rz1WP/src/animation.jl:156

True World State

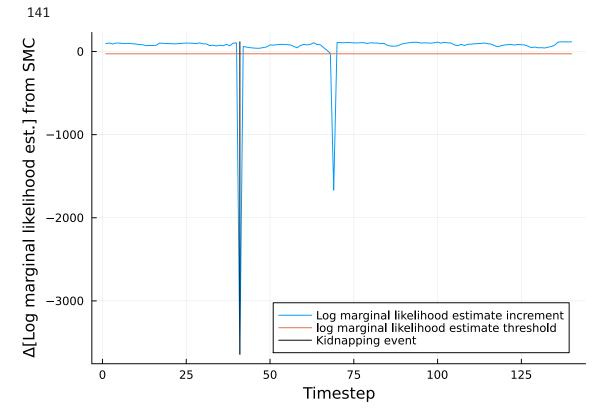
Agent Beliefs







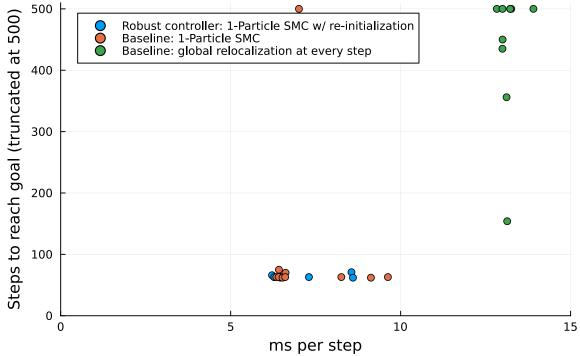
Plotting the log marginal likelihood estimates from each timestep:



In [52]:

Plotting the runtime and effectiveness of each controller

```
I[[CC] III
          includet("KidnappedRobot/measure_performance.jl") # Loads `take_measuremel
In [54]:
          robust costs runtimes = [take measurement(rollout model) for =1:10];
In [55]:
          baseline1 costs runtimes = [take measurement(baseline rollout model) for
In [56]:
          baselinepf costs runtimes = [take measurement(baseline pf rollout model)
In [57]:
          plot(;
              title="Controller performance comparison [no kidnapping]",
              ylabel="Steps to reach goal (truncated at 500)",
              xlabel="ms per step",
              vlims=(0, 510),
              xlims=(0,15)
          scatter!(map(x->x[2]*1000, robust_costs_runtimes), map(x->x[1], robust_costs_runtimes)
          scatter!(map(x->x[2]*1000, baselinepf_costs_runtimes), map(x->x[1], basel
          scatter!(map(x->x[2]*1000, baseline1 costs runtimes), map(x->x[1], baseline1 costs runtimes)
              Controller performance comparison [no kidnapping]
```



```
In [58]:
           robust_costs_runtimes_KR = [take_measurement_KR(rollout_model) for _=1:10
In [59]:
          baseline1_costs_runtimes_KR = [take_measurement_KR(baseline_rollout_model
In [60]:
          baselinepf_costs_runtimes_KR = [take_measurement_KR(baseline_pf_rollout_measurement_KR)
In [61]:
          plot(:
               +i+lo-"Controllor norformance comparison [with kidnapping]"
```